

Starptautiskā konkursa "Kengurs" uzdevumi

20.	Three three-digits frumbers are formed from digits from 1 to 5 (each digit is used exactly							
	once). Which of the following numbers couldn't be equal to the sum of this three numbers?					24.03.2016.		
	(A) 1500	(B) 1503	(C) 1512	(D) 1521	(E) 1575			
26		atadiata Caus	3 point pro					

26. A cube is dissected into 6 pyramids by connecting a given point in the interior of the cube with each vertex of the cube. The volumes of five of these pyramids are 2, 5, 10, 11 and 14. What is the volume of the sixth pyramid? (D) 9

25. Three three digits numbers are formed from digits from 1 to 0 (each digit is used exactly

(A) 1(B) 4 (C) 6

(E) 12

27. A fortress is surrounded by a wall that is 2016 meters long. There are enemy watch towers every other 8 meters on the wall. Besides, every 64 meters the shape of the enemy watch tower is repeated. What is the maximum different shape number of enemy watch towers? (A) 1 (B) 2 (D) 6 (C) 4(E) 8

28. Ann chose a positive integer n and wrote down the sum of all positive integers from 1 to n. A prime number p divides the sum, but not any of the summands. Which of the following

could be n + p? (A) 217

(B) 221

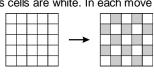
(C) 229

(D) 245

(E) 269

29. Consider a 5 × 5 square divided into 25 cells. Initially all its cells are white. In each move

it is allowed to change the color of any three consecutive cells in a row or in a column to the opposite color (i.e. white cells become black and black ones become white). What is the smallest possible number of moves needed to obtain the chessboard coloring shown in the figure?



(A)less than 10

(B) 10

(C) 12

(D) more than 12

(E) It is impossible to do

30. The positive integer N has exactly six distinct (positive) divisors including 1 and N. The product of five of these is 648. Which one of the following is the sixth divisor of N?

(A) 4

(B) 8

(C)9

(D) 12

(E) 24

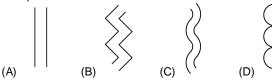
Laiks uzdevumu risināšanai - 75 minūtes!

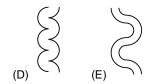
1. The sum of the ages of Tom and John is 23, the sum of the ages of John and Alex is 24 and the sum of the ages of Tom and Alex is 25. What is the age of the oldest one? (A) 10 (B) 11 (C) 12 (D) 13 (E) 14

2. The sum of $\frac{1}{10} + \frac{1}{100} + \frac{1}{1000}$ is (A) $\frac{3}{111}$ (B) $\frac{100}{1110}$

11.-12. klases

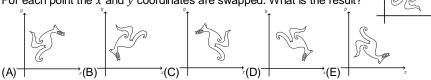
3. Maria wants to build a bridge across a river and knows that the shortest possible bridge from each point on one shore is always of the same length. Which of these pictures cannot be a picture of her river?





4. How many integers are greater than 2015 · 2017 but less than 2016 · 2016? (B) 1 (C) 2015 (D) 2016 (E) 2017 (A) 0

5. A set of points forms a picture of a kangaroo in the xy-plane as shown. For each point the x and y coordinates are swapped. What is the result?



What is the smallest number of planes that are needed to enclose a bounded part in threedimensional space?

(A) 3

(B) 4

(C) 5

(D) 6

(E) 7

7. Ann wants to write nine integers into the circles on the diagram so that, for the eight small triangles whose vertices are joined by segments the sums of the numbers in their vertices are identical. What is the largest number of different integers she can use?

(A) 1

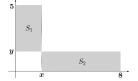
(B) 2

(C)3

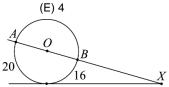
(D) 5

(E) 8

- 8. The rectangles S_1 and S_2 in the picture have the same area. Determine the ratio $\frac{x}{-}$.
 - (A) 1
- (B) $\frac{3}{2}$ (C) $\frac{4}{3}$ (D) $\frac{7}{4}$
- $(E)^{\frac{8}{5}}$



- 9. If $x^2 4x + 2 = 0$, then $x + \frac{2}{x}$ equals
 - (A) -4
- (B) -2
- (D) 2



- 10. The lengths of arc AP and arc BP in the figure are 20 and 16 respectively. Then the value of the angle AXP equals
 - (A) 30°
- (B) 24° (D) 15°
- $(C) 18^{\circ}$

(E) 10°

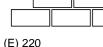
4 point problems

- 11. a, b, c, d are positive integers satisfying $a + 2 = b 2 = c \cdot 2 = d$: 2. Which is the largest of the four numbers a, b, c and d?
 - (A) a
- (B) b

- (D) d
- (E) This is not uniquely determined.
- 12. In this figure each upper field is the product of the two fields directly underneath. Which of the following numbers cannot appear in the top field, if the three bottom fields only contain natural numbers bigger than 1?



- (B) 84
- (C) 90
- (D) 105



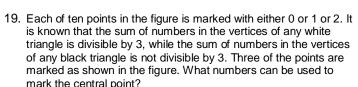
- 13. What is x_4 , if $x_1 = 2$ and $x_{n+1} = x_n^{x_n}$ for n > 1?

 (A) 2^{2^3} (B) 2^{2^4} (C) $2^{2^{11}}$ (D) $2^{2^{16}}$

- (E) $2^{2^{768}}$
- 14. In rectangle ABCD the length of the side BC is half the length of the diagonal AC. Let M be a point on CD such that AM = MC. What is the size of angle CAM?
 - (A) 12.5°
- (B) 15°
- (C) 27.5°
- (D) 42.5°
- (E) some other angle
- 15. Diana cut up a rectangle of area 2016 into 56 equal squares. The lengths of the sides of the rectangle and of the squares are integers. From how many different rectangles is it possible for her to do this?
 - (A) 2
- (B) 4
- (C) 6
- (D) 8
- (E) 0
- 16. On the Island of Knights and Knaves every citizen is either a Knight (who always speaks the truth) or a Knave (who always lies). During your travels on the island you meet 7 people sitting around a bonfire. They all tell you "I'm sitting between two Knaves!" How many Knaves are there?
 - (A) 3
- (B) 4
- (C) 5

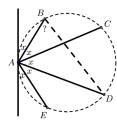
- (D) 6
- (E) You need more information to determine this

- 17. The equations $x^2 + ax + b = 0$ and $x^2 + bx + a = 0$ both have real roots. It is known that the sum of squares of the roots of the first equation is equal to the sum of squares of the roots of the second one, and $a \neq b$. Then a + b equals
 - (A) 0(C) 4
- (B) -2
- (D) -4
- (E) It is impossible to determine
- 18. If the perimeter of the square in the figure equals 4 then the perimeter of the equilateral triangle equals
 - (A) 4 (C) 3
- (B) 3 + $\sqrt{3}$
- (D) $3 + \sqrt{2}$ (E) $4 + \sqrt{3}$



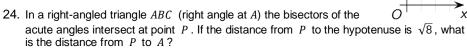


- (A) Only 0.
- (B) Only 1.
- (C) Only 2.
- (D) Only 0 and 1.
- (E) It is impossible to determine
- 20. Beting draws five points A.B.C.D and E on a circle as well as the tangent to the circle at A, such that all five angles marked with x are equal. (Note that the drawing is not to scale.) How large is the angle ABD?
 - (A) 66°
- (B) 70.5°
- (C) 72°
- (D) 75°
- (E) 77.5°



5 point problems

- 21. How many different solutions are there to the equation $(x^2 4x + 5)^{x^2 + x 30} = 1$?
 - (A) 1
- (B) 2
- (C) 3
- (D) 4
- (E) infinitely many
- 22. A quadrilateral contains an inscribed circle (i.e. a circle tangent to the four sides of the quadrilateral). The ratio of the perimeter of the quadrilateral to that of the circle is 4:3. Then the ratio of the area of the quadrilateral to that of the circle is
 - (A) $4: \pi$
- (B) $3\sqrt{2}$: π
- (C) 16: 9
- (D) π : 3
- (E) 4: 3
- 23. How many quadratic functions in x have a graph passing through at least 3 of the marked points?
 - (A) 6
- (B) 15
- (C) 19
- (D) 22



- (A) 8
- (B) 3
- (C) $\sqrt{10}$
- (D) $\sqrt{12}$
- (E) 4